

### Exercise sheet 2

(Due: Wednesday, 18. January at noon, best via email to dm@ling.ohio-state.edu)

Provide PROLOG definitions for the following relations. Please test before handing them in.

1. `last/2`: a two place relation which takes a list as first argument and returns the last element of that list (if there is one) as second argument; i.e., `last(+List,-Last-List-element)`

Example queries:

- `?- last([a,b,c,d],X). => X=d`
- `?- last([a,b,c],X). => X=c`
- `?- last([],X). => no`

2. `firstLastSwap/2`: a two place relation which takes a list and returns the same list with one difference: the first list element and the last list element are exchanged; i.e., `firstLastSwap(+List,-List-With-First-Last-Swapped)`

Example queries:

- `?- firstLastSwap([a,b,c,d],X). => [d,b,c,a]`
- `?- firstLastSwap([a,b,c],X). => [c,b,a]`
- `?- firstLastSwap([],X). => no`

3. `delete_a/2`: a two place relation which takes a list and deletes one first occurrence of a (if there is one); i.e., `delete_a(+List,-List-with-one-a-less)`

Example queries:

- `?- delete_a([a,b,a,d],X). => X=[b,a,d]; X=[a,b,d]`
- `?- delete_a([b,a,c,a,g,h],X). => X=[b,c,a,g,h]; X=[b,a,c,g,h]`
- `?- delete_a([b,g,a],X). => X=[b,g]`
- `?- delete_a([b,g,a,a],X). => X=[b,g,a]; X=[b,g,a]`
- `?- delete_a([b,c],X). => X=[b,c]`

Could you also write the relation so that it only removes the first occurrence of an a as exemplified below? What is needed to do this?

- `?- delete_a([a,b,a,d],X). => X=[b,a,d]`
- `?- delete_a([b,a,c,a,g,h],X). => X=[b,c,a,g,h]`
- `?- delete_a([b,g,a],X). => X=[b,g]`
- `?- delete_a([b,g,a,a],X). => X=[b,g,a]`
- `?- delete_a([b,c],X). => X=[b,c]`

4. `containsList/2`: a two place relation which succeeds if the second list is part of the first; i.e., `containsList(+List,+Sublist)`

Example queries:

- `?- containsList([a,b,c,d],[b,c]).`  $\Rightarrow$  yes
- `?- containsList([a,b,b,c,d],[b,c]).`  $\Rightarrow$  yes
- `?- containsList([a,b,c,d],[a,b]).`  $\Rightarrow$ yes
- `?- containsList([a,b,c,d],[a,b,c]).`  $\Rightarrow$  yes
- `?- containsList([a,b,c,d],[a]).`  $\Rightarrow$  yes
- `?- containsList([a,b,c,d],[ ]).`  $\Rightarrow$  no
- `?- containsList([a,b,c,d],[a,c]).`  $\Rightarrow$  no
- `?- containsList([a,b,c,d],[b,d]).`  $\Rightarrow$  no

5. `permute/2`: a two place relation which takes a list as its first argument and returns as second argument each list that consists of all and only the elements of the input list in any order of occurrence; i.e., `permute(+List,-Permuted-list)`

Example queries:

- `?- permute([a,b],X).`  $\Rightarrow$  `X=[a,b]` ; `X=[b,a]`

Hint: in defining `permute` it is useful to define an auxiliary relation `insert` which inserts a single element into an input list at any arbitrary position of the list and returns this newly constructed list.