

More on implementing finite state machines in PROLOG

- Recursive relations in PROLOG:
 - data structures needed
 - two example relations
- Completing the FSM recognition and generation algorithms to use
 - ϵ transitions
 - abbreviations

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Recursive relations in PROLOG Compound terms as data structures

To define recursive relations, one needs a richer data structure than the constants (atoms) introduced so far: *compound terms*.

A compound term comprises a functor and a sequence of one or more terms, the argument.¹ Compound terms are standardly written in prefix notation.²

For example:

- `bin_tree(mother, l-dtr, r-dtr)`
- `bin_tree(s, np, bin_tree(vp,v,n))`

¹An atom can be thought of as a functor with arity 0.

²Infix and postfix operators can also be defined, but need to be declared.

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Recursive relations in PROLOG Lists as special compound terms

Lists are represented as compound terms.

- symbol "." as binary functor
- first argument: first element of list
- second argument: rest of list
- empty list: represented by the atom "[]"

Example: `.(a, .(b, .(c, .(d, [])))`

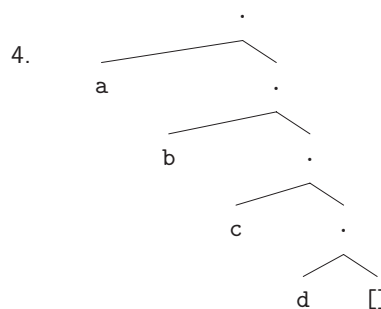
Abbreviatory syntax available:

- bracket notation: `[element1 | restlist]`
Example: `[a | [b | [c | [d | []]]]]`
- element separator: `[element1 , element2]`
= `[element1 | [element2 | []]]`
Example: `[a, b, c, d]`

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Four equivalent representations for lists:

1. `[a,b,c,d]`
2. `[a | [b | [c | [d | []]]]]`
3. `.(a, .(b, .(c, .(d, [])))`



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Recursive relations in PROLOG

Example relations I: append

- Idea: a relation concatenating two lists
- Example:
?- append([a,b,c],[d,e],X).
⇒ X=[a,b,c,d,e]

```
append([],L,L).  
append([H|T],L,[H|R]) :-  
    append(T,L,R).
```

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Recursive relations in PROLOG

Example relations II: reverse

- Idea: reverse a list
- Example: ?- reverse([a,b,c],X). ⇒ X=[c,b,a]

1. naive reverse:

```
naive_reverse([],[]).  
naive_reverse([H|T],Result) :-  
    naive_reverse(T,Aux),  
    append(Aux,[H],Result).
```

2. reverse:

```
reverse(A,B) :-  
    reverse_aux(A,[],B).  
  
reverse_aux([],L,L).  
reverse_aux([H|T],L,Result) :-  
    reverse_aux(T,[H|L],Result).
```

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Negation in PROLOG

- PROLOG does not have the means to express not(P) in the sense that P is known to be false.
- Instead, PROLOG has so-called *negation by failure*. Negating a goal P in PROLOG means that the system will try to prove P and if that fails, not(P) will be true.
- As notation for negation, the unary operator \+ is used. To use the functor not instead, one can simply define: not(X) :- \+(X).

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FSMs with ϵ transitions and abbreviations

Defining PROLOG representations

1. Decide on a symbol to use to mark ϵ transitions: '#'
2. Define abbreviations for labels:
macro(Label,Word).
3. Define a relation special/1 to recognize abbreviations and epsilon transitions:

```
special(#).  
special(X) :-  
    macro(X,_).
```

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FSMs with ϵ transitions and abbreviations

Extending the recognition algorithm

```
test(Words) :-
    initial(Node),
    recognize(Node,Words).

recognize(Node,[]) :-
    final(Node).
recognize(FromNode,String) :-
    arc(FromNode,Label,ToNode),
    traverse(Label,String,NewString),
    recognize(ToNode,NewString).

traverse(Label,[Label|RestString],RestString) :-
    not(special(Label)).
traverse(Abbrev,[Label|RestString],RestString) :-
    macro(Abbrev,Label).
traverse('#',String,String).

special(#).
special(X) :-
    macro(X,_).

not(X) :- \+(X).
```