

Introduction to Parsing

Detmar Meurers: Intro to Computational Linguistics I
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Overview

- What is a parser?
- Under what criteria can they be evaluated?
- Parsing strategies
 - top-down vs. bottom-up
 - left-right vs. right-left
 - depth-first vs. breadth-first
- Implementing different types of parsers:
 - Basic top-down and bottom-up
 - More efficient algorithms

Parsers and criteria to evaluate them

- Function of a parser:
 - grammar + string \rightarrow analysis trees
- Main criteria for evaluating parsers:
 - correctness
 - completeness
 - efficiency

Correctness

A parser is **correct** iff for every grammar and for every string, every analysis returned by parser is an actual analysis.

Correctness is nearly always required (unless simple post-processor could eliminate wrong analyses)

Completeness

A parser is **complete** iff for every grammar and for every string, every correct analysis is found by the parser.

- In theory, always desirable.
- In practice, essential to find the 'relevant' analysis first (possibly using heuristics).
- For grammars licensing an infinite number of analyses this means: there is no analysis that the parser could not find.

Efficiency

- One can reason about complexity of (parsing) algorithms by considering how it will deal with bigger and bigger examples.
- For practical purposes, the factors ignored by such analyses are at least as important.
 - profiling using typical examples important
 - finding the (relevant) first parse vs. all parse
- Memoization of complete or partial results is essential to obtain efficient parsing algorithms.

Complexity classes

If n is the length of the string to be parsed, one can distinguish the following complexity classes:

- **constant**: amount of work does not depend on n
- **logarithmic**: amount of work behaves like $\log_k(n)$ for some constant k
- **polynomial**: amount of work behaves like n^k , for some constant k . This is sometimes subdivided into the cases
 - **linear** ($k = 1$)
 - **quadratic** ($k = 2$)
 - **cubic** ($k = 3$)
 - . . .
- **exponential**: amount of work behaves like k^n , for some constant k .

Complexity and the Chomsky hierarchy

Grammar type	Worst-case complexity of recognition
regular (3)	linear
context-free (2)	cubic (n^3)
context-sensitive (1)	exponential
general rewrite (0)	undecidable

Recognition with type 0 grammars is **recursively enumerable**: if a string x is in the language, the recognition algorithm will succeed, but it will not return if x is not in the language.

Parsing strategies

1. What do we start from?
 - top-down vs. bottom-up
2. In what order is the string or the RHS of a rule looked at?
 - left-to-right, right-to-left, island-driven, . . .
3. How are alternatives explored?
 - depth-first vs. breadth-first

Direction of processing I: Top-down

Goal-driven processing is Top-down:

- Start with the start symbol
- Derive sentential forms.
- If the string is among the sentences derived this way, it is part of the language.

Direction of processing II: Bottom-up

Data-driven processing is Bottom-up:

- Start with the sentence.
- For each substring σ of each sentential form $\alpha\sigma\beta$, find each grammar rule $N \rightarrow \sigma$ to obtain all sentential forms $\alpha N\beta$.
- If the start symbol is among the sentential forms obtained, the sentence is part of the language.

Problem: Epsilon rules ($N \rightarrow \epsilon$).

The order in which one looks at a RHS

Left-to-Right

- Use the leftmost symbol first, continuing with the next to its right

How are alternatives explored? I. Depth-first

- At every choice point: Pursue a single alternative completely before trying another alternative.
- State of affairs at the choice points needs to be remembered. Choices can be discarded after unsuccessful exploration.
- Depth-first search is not necessarily complete.

Problem for top-down, left-to-right, depth-first processing:

- left-recursion
For example, a rule like $N' \rightarrow N' PP$ leads to non-termination.

How are alternatives explored? II. Breadth-first

- At every choice point: Pursue every alternative for one step at a time.
- Requires serious bookkeeping since each alternative computation needs to be remembered at the same time.
- Search is guaranteed to be complete.

Compiling and executing DCGs in Prolog

- DCGs are a grammar formalism supporting any kind of parsing regime.
- The standard translation of DCGs to Prolog plus the proof procedure of Prolog results in a parsing strategy which is
 - top-down
 - left-to-right
 - depth-first

Implementing parsers

- Data structures: a parser configuration
- Top-down parsing
 - formal characterization
 - Prolog implementation
- Bottom-up parsing
 - formal characterization
 - Prolog implementation
- Towards more efficient parsers:
 - Left-corner
 - Remembering subresults

An example grammar (parser/simple/grammar.pl)

```
% defining grammar rule operator
:- op(1100,xfx,'--->').
```

```
% lexicon:
```

```
vt ---> [saw].
det ---> [the].
det ---> [a].
n ---> [dragon].
n ---> [boy].
adj ---> [young].
```

```
% syntactic rules:
```

```
s ---> [np, vp].
vp ---> [vt, np].
np ---> [det, n].
n ---> [adj, n].
```

A parser configuration

Assuming a left-to-right order of processing, a **configuration** of a parser can be encoded by a pair of

- a stack as auxiliary memory
- the string remaining to be recognized

More formally, for a grammar $G = (N, \Sigma, S, P)$, a parser configuration is a pair $\langle \alpha, \tau \rangle$ with $\alpha \in (N \cup \Sigma)^*$ and $\tau \in \Sigma^*$

Top-down parsing

- **Start configuration** for recognizing a string ω : $\langle S, \omega \rangle$
- **Available actions**:
 - **consume**: remove an expected terminal a from the string
 $\langle a\alpha, a\tau \rangle \mapsto \langle \alpha, \tau \rangle$
 - **expand**: apply a phrase structure rule
 $\langle A\beta, \tau \rangle \mapsto \langle \alpha\beta, \tau \rangle$ if $A \rightarrow \alpha \in P$
- **Success configuration**: $\langle \epsilon, \epsilon \rangle$

A top-down parser in Prolog (parser/simple/td_parser.pl)

```
:- op(1100,xfx,'--->').

% Start
td_parse(String) :- td_parse([s],String).

% Success
td_parse([],[]).

% Consume
td_parse([H|T],[H|R]) :-
    td_parse(T,R).

% Expand
td_parse([A|Beta],String) :-
    (A ---> Alpha),
    append(Alpha,Beta,Stack),
    td_parse(Stack,String).
```

Top-Down, left-right, depth-first tree traversal

S_1

$S \rightarrow NP VP$
 $VP \rightarrow Vt NP$
 $NP \rightarrow Det N$
 $N \rightarrow Adj N$

$Vt \rightarrow \text{saw}$
 $Det \rightarrow \text{the}$
 $Det \rightarrow \text{a}$
 $N \rightarrow \text{dragon}$
 $N \rightarrow \text{boy}$
 $Adj \rightarrow \text{young}$

Top-Down, left-right, depth-first tree traversal

S_1

NP_2

$S \rightarrow NP VP$
 $VP \rightarrow Vt NP$
 $NP \rightarrow Det N$
 $N \rightarrow Adj N$

$Vt \rightarrow \text{saw}$
 $Det \rightarrow \text{the}$
 $Det \rightarrow \text{a}$
 $N \rightarrow \text{dragon}$
 $N \rightarrow \text{boy}$
 $Adj \rightarrow \text{young}$

Top-Down, left-right, depth-first tree traversal

S_1

NP_2

Det_3

$S \rightarrow NP VP$
 $VP \rightarrow Vt NP$
 $NP \rightarrow Det N$
 $N \rightarrow Adj N$

$Vt \rightarrow \text{saw}$
 $Det \rightarrow \text{the}$
 $Det \rightarrow \text{a}$
 $N \rightarrow \text{dragon}$
 $N \rightarrow \text{boy}$
 $Adj \rightarrow \text{young}$

Top-Down, left-right, depth-first tree traversal

S_1

NP_2

Det_3



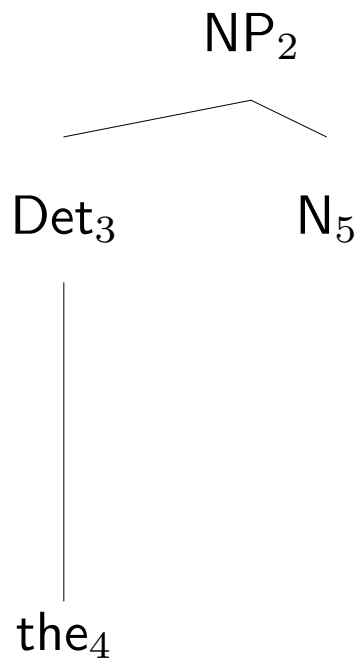
the_4

$S \rightarrow NP VP$
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 $N \rightarrow Adj N$

$Vt \rightarrow saw$
 $Det \rightarrow the$
 $Det \rightarrow a$
 $N \rightarrow dragon$
 $N \rightarrow boy$
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Top-Down, left-right, depth-first tree traversal

S_1

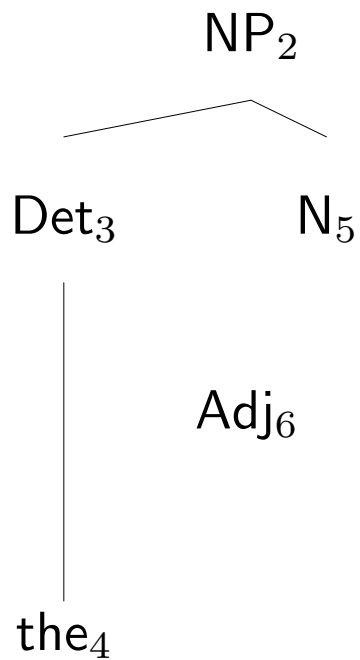


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Top-Down, left-right, depth-first tree traversal

S_1

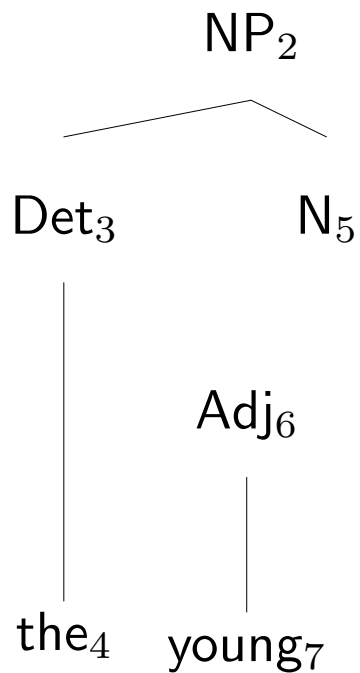


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Top-Down, left-right, depth-first tree traversal

S_1

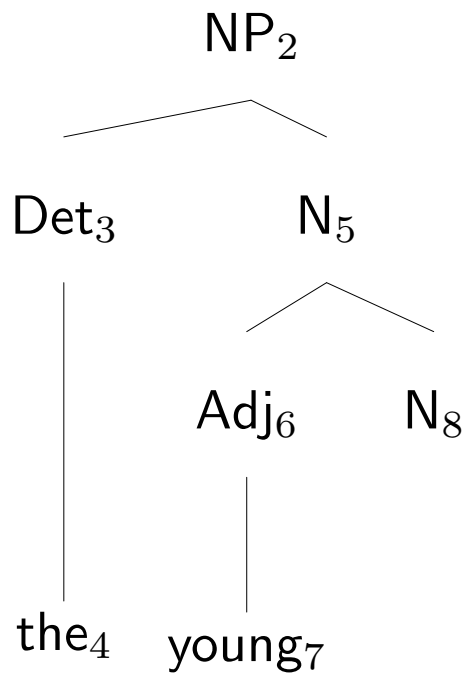


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Top-Down, left-right, depth-first tree traversal

S_1

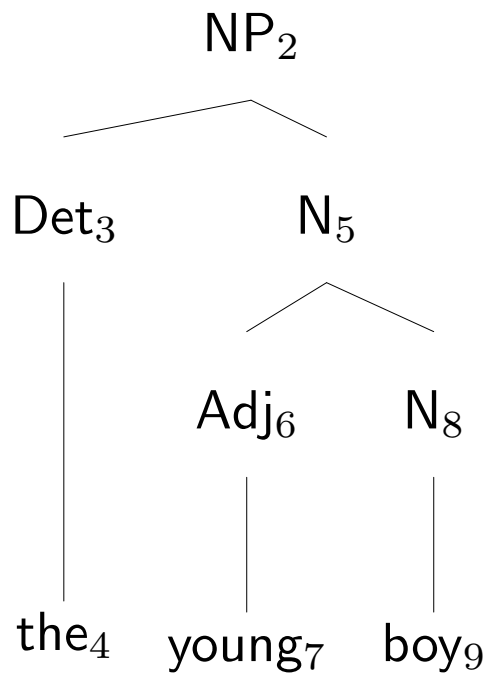


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Top-Down, left-right, depth-first tree traversal

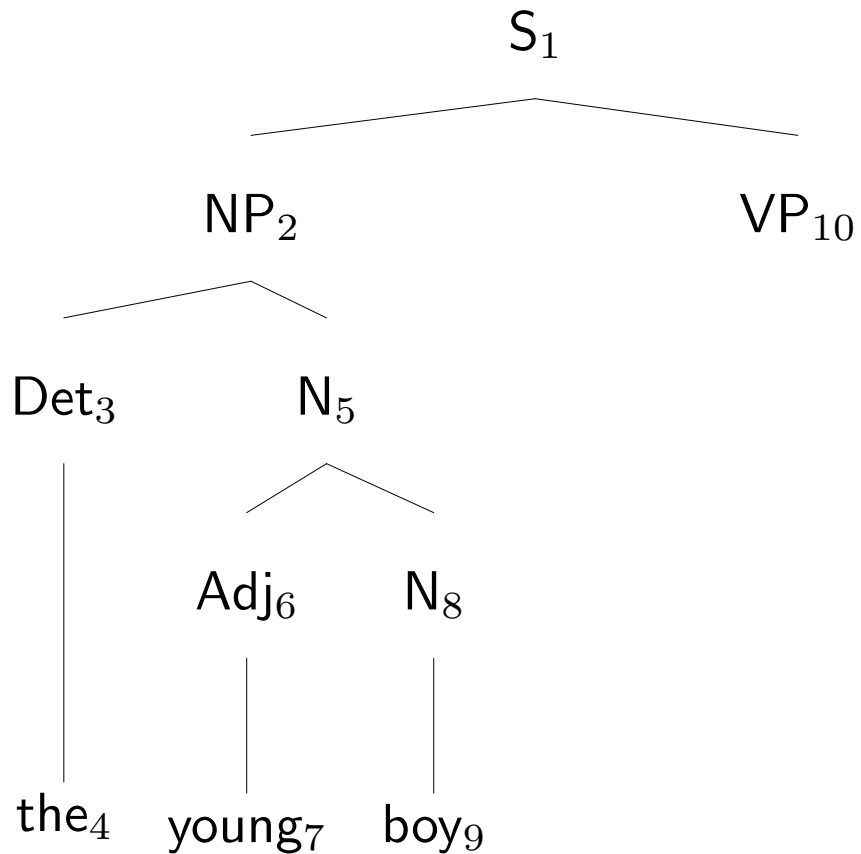
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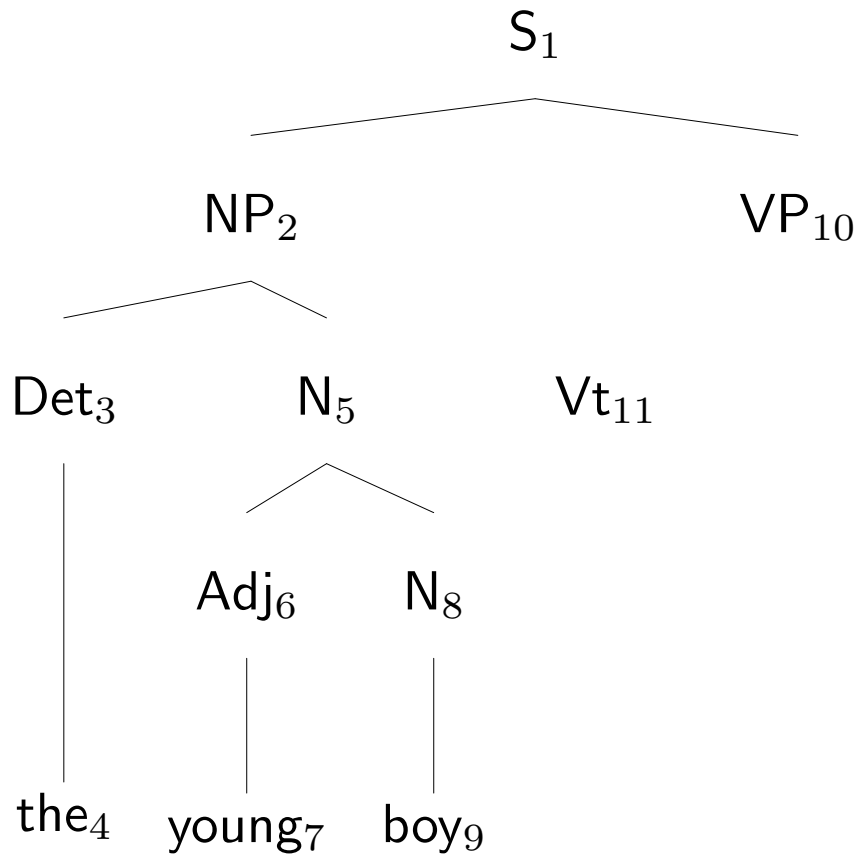
Top-Down, left-right, depth-first tree traversal



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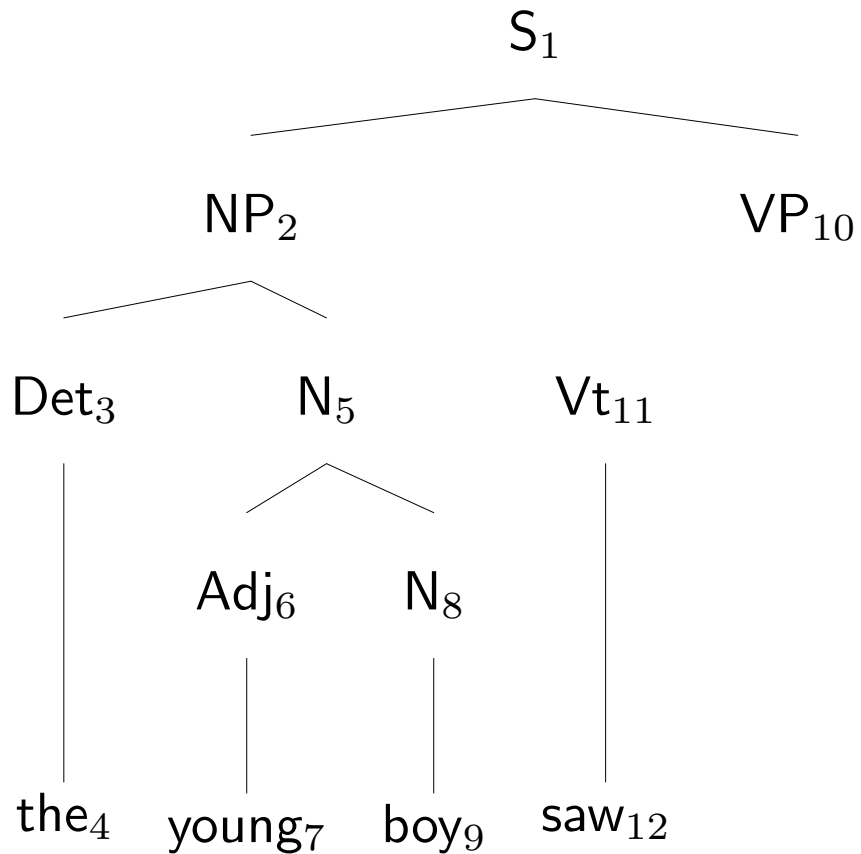
Top-Down, left-right, depth-first tree traversal



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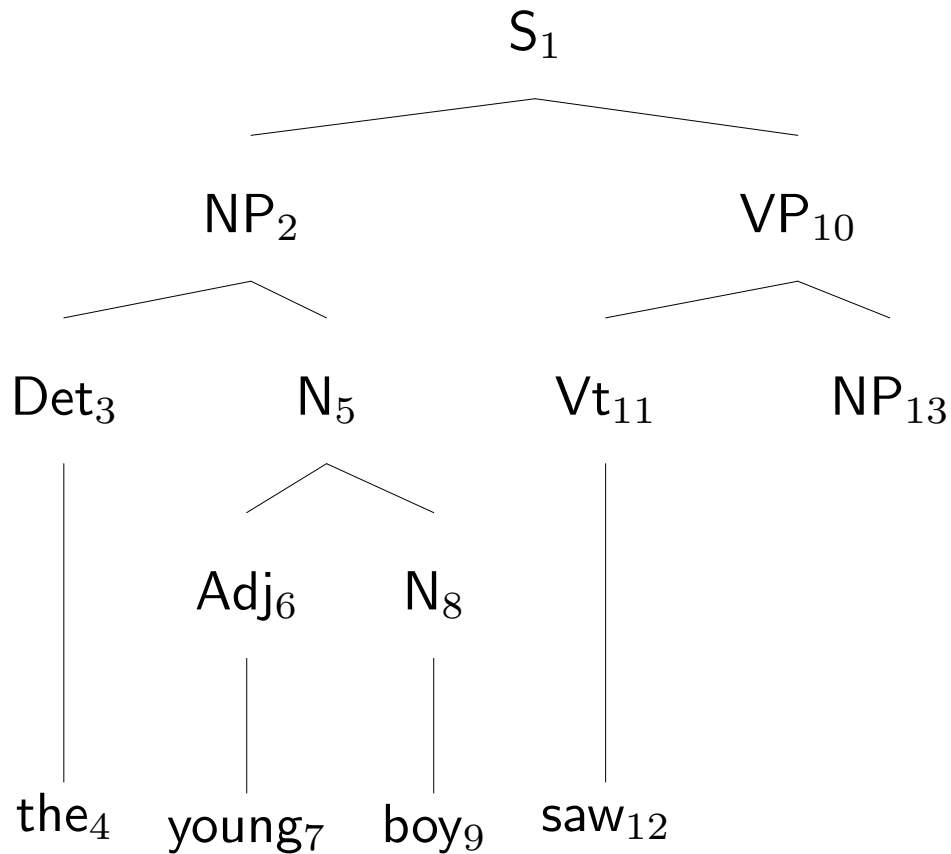
Top-Down, left-right, depth-first tree traversal



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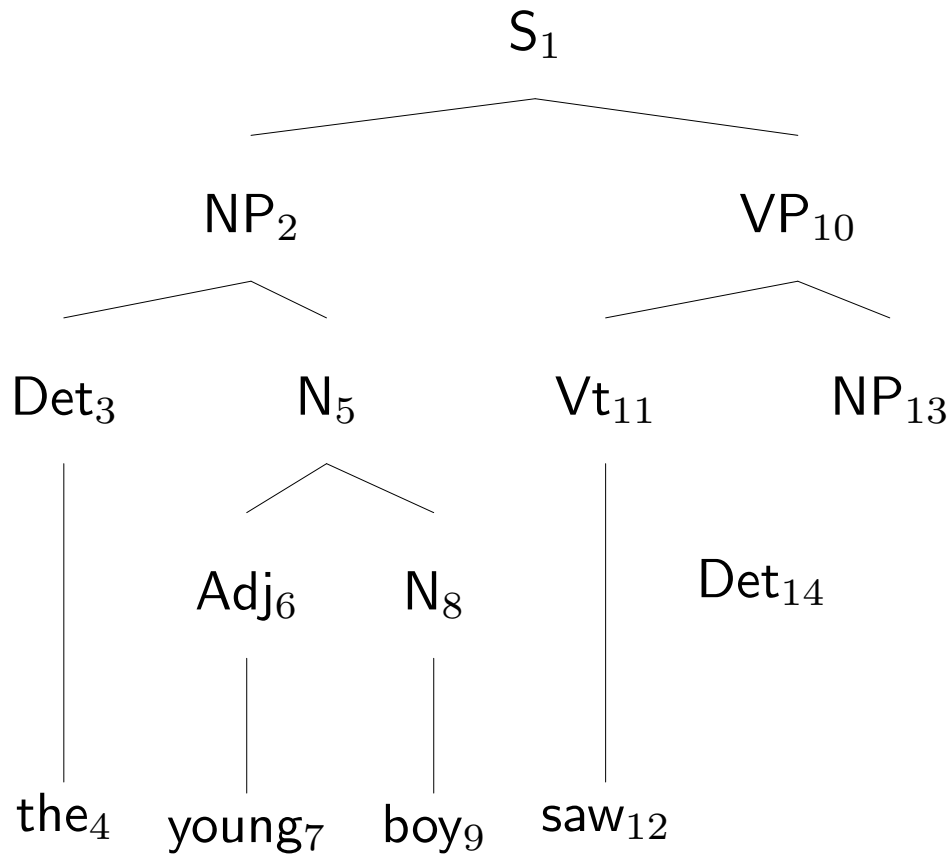
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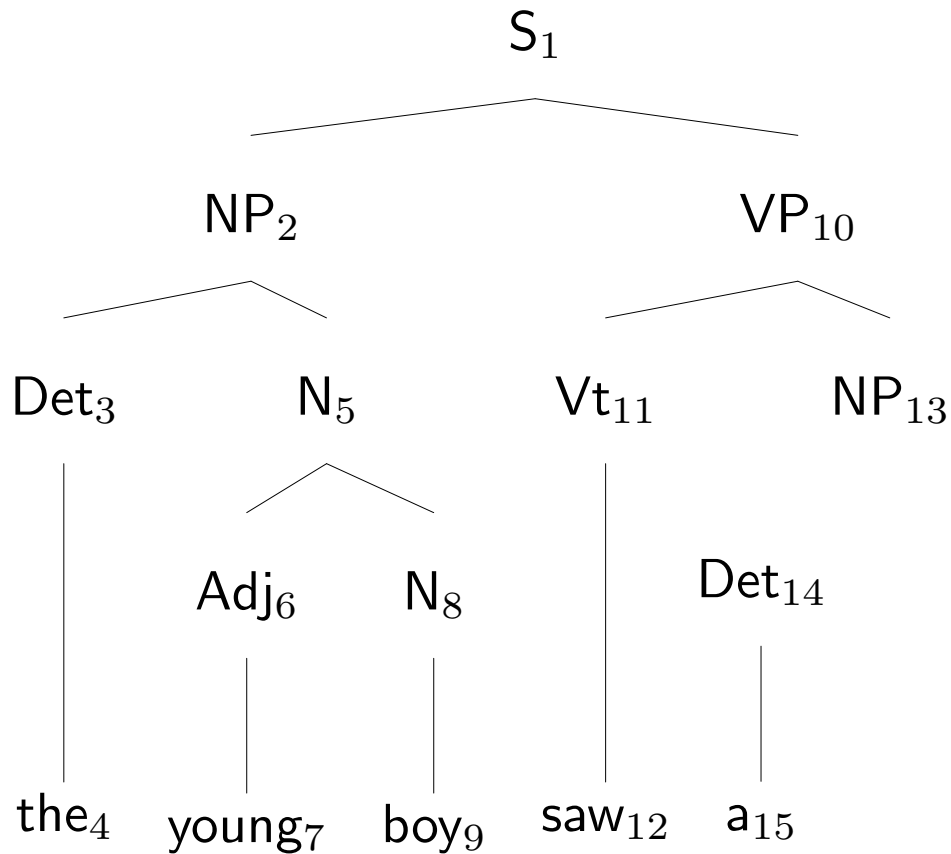
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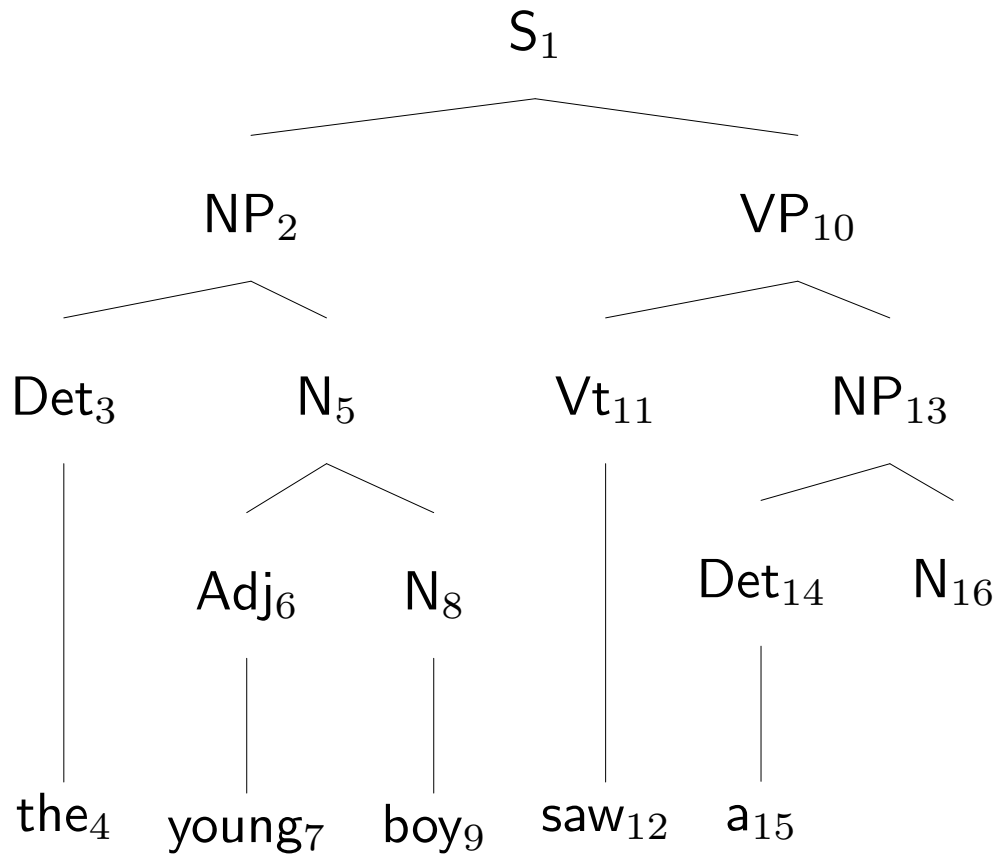
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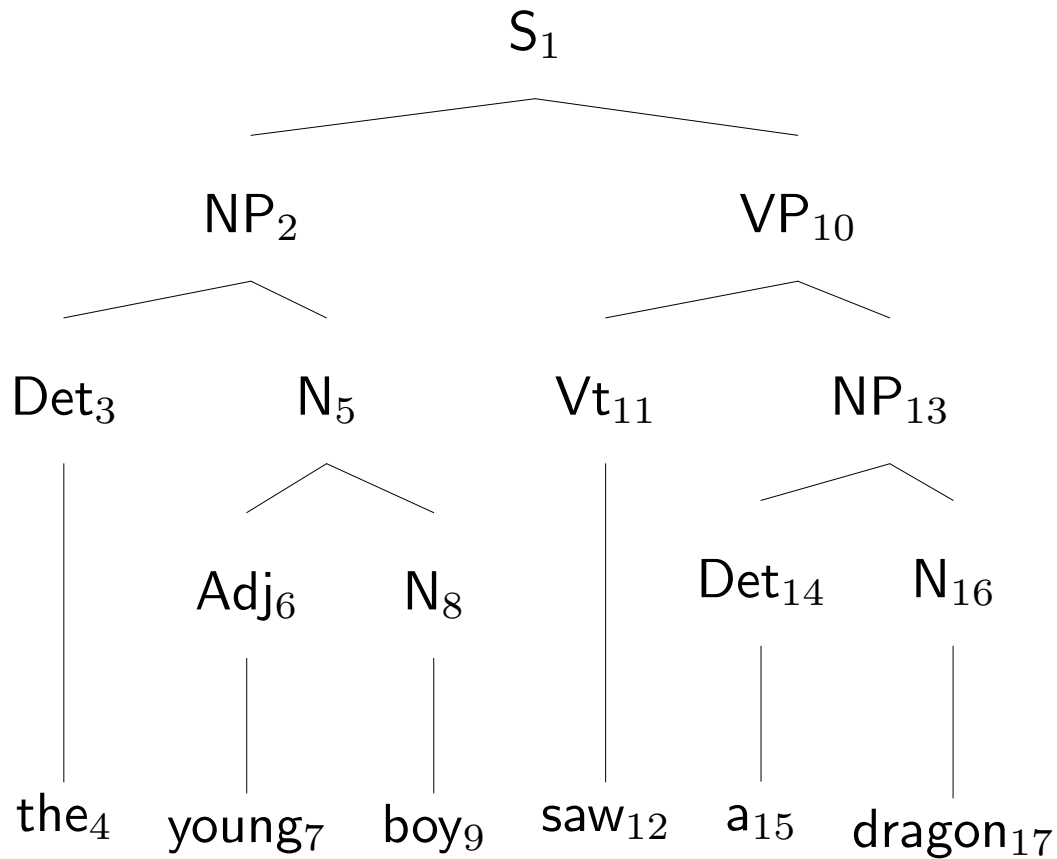
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Top-Down, left-right, depth-first tree traversal



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A trace (parser/simple/grammar.pl, parser/simple/td_parser_trace.pl)

```
?- td_parse([the,young,boy,saw,the,dragon]).  
< [s], [the, young, boy, saw, the, dragon] >  
< [np, vp], [the, young, boy, saw, the, dragon] >  
< [det, n, vp], [the, young, boy, saw, the, dragon] >  
< [the, n, vp], [the, young, boy, saw, the, dragon] >  
< [n, vp], [young, boy, saw, the, dragon] >  
< [dragon, vp], [young, boy, saw, the, dragon] >  
< [boy, vp], [young, boy, saw, the, dragon] >  
< [adj, n, vp], [young, boy, saw, the, dragon] >  
< [young, n, vp], [young, boy, saw, the, dragon] >  
< [n, vp], [boy, saw, the, dragon] >  
< [dragon, vp], [boy, saw, the, dragon] >  
< [boy, vp], [boy, saw, the, dragon] >  
< [vp], [saw, the, dragon] >
```

< [vt, np], [saw, the, dragon] >
< [saw, np], [saw, the, dragon] >
< [np], [the, dragon] >
< [det, n], [the, dragon] >
< [the, n], [the, dragon] >
< [n], [dragon] >
< [dragon], [dragon] >
< [], [] >

Bottom-up parsing

- **Start configuration** for recognizing a string ω : $\langle \epsilon, \omega \rangle$
- **Available actions:**
 - **shift:** turn to the next terminal a of the string
 $\langle \alpha, a\tau \rangle \mapsto \langle \alpha a, \tau \rangle$
 - **reduce:** apply a phrase structure rule
 $\langle \beta\alpha, \tau \rangle \mapsto \langle \beta A, \tau \rangle$ if $A \rightarrow \alpha \in P$
- **Success configuration:** $\langle S, \epsilon \rangle$

A shift-reduce parser in Prolog (parser/simple/sr_parser.pl)

```
:- op(1100,xfx,'--->').

sr_parse(String) :- sr_parse([],String).      % Start

sr_parse([s],[]).                             % Success

sr_parse(Stack,String) :-                     % Reduce
    append(Beta,Alpha,Stack),
    (A ---> Alpha),
    append(Beta,[A],NewStack),
    sr_parse(NewStack,String).

sr_parse(Stack,[Word|String]) :-             % Shift
    append(Stack,[Word],NewStack),
    sr_parse(NewStack,String).
```

Bottom-up, left-right, depth-first tree traversal

$S \rightarrow NP VP$
 $VP \rightarrow Vt NP$
 $NP \rightarrow Det N$
 $N \rightarrow Adj N$

$Vt \rightarrow \text{saw}$
 $Det \rightarrow \text{the}$
 $Det \rightarrow \text{a}$
 $N \rightarrow \text{dragon}$
 $N \rightarrow \text{boy}$
 $Adj \rightarrow \text{young}$

the₁

Bottom-up, left-right, depth-first tree traversal

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Det₂

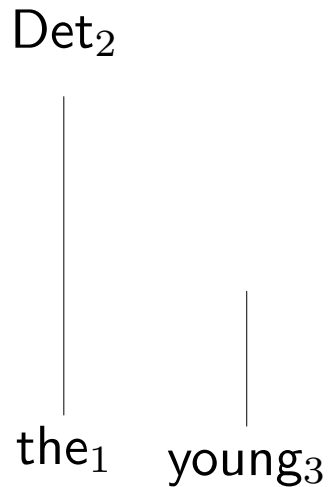


the₁

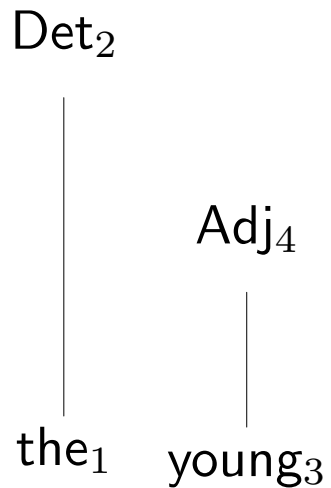
Bottom-up, left-right, depth-first tree traversal

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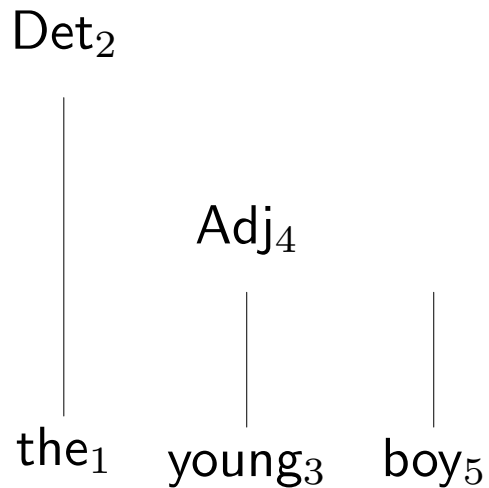
Bottom-up, left-right, depth-first tree traversal



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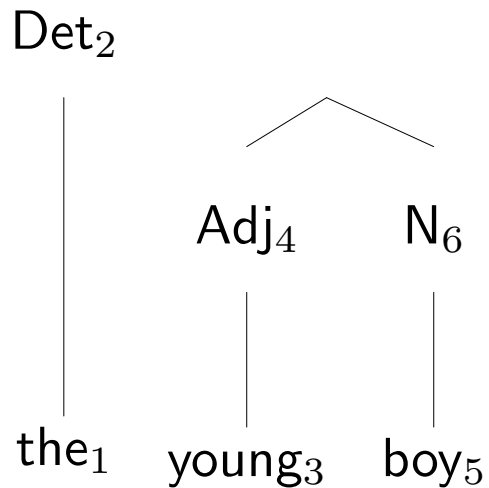
Bottom-up, left-right, depth-first tree traversal



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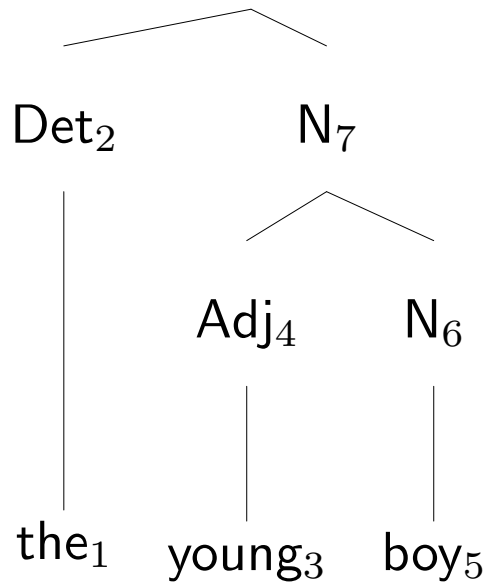
Bottom-up, left-right, depth-first tree traversal



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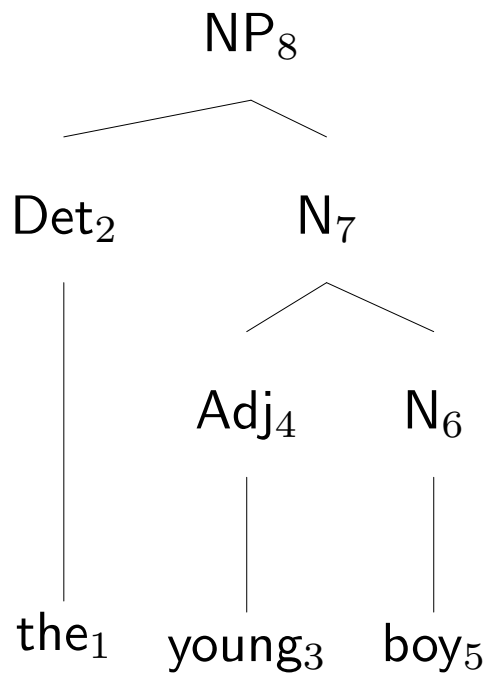
Bottom-up, left-right, depth-first tree traversal



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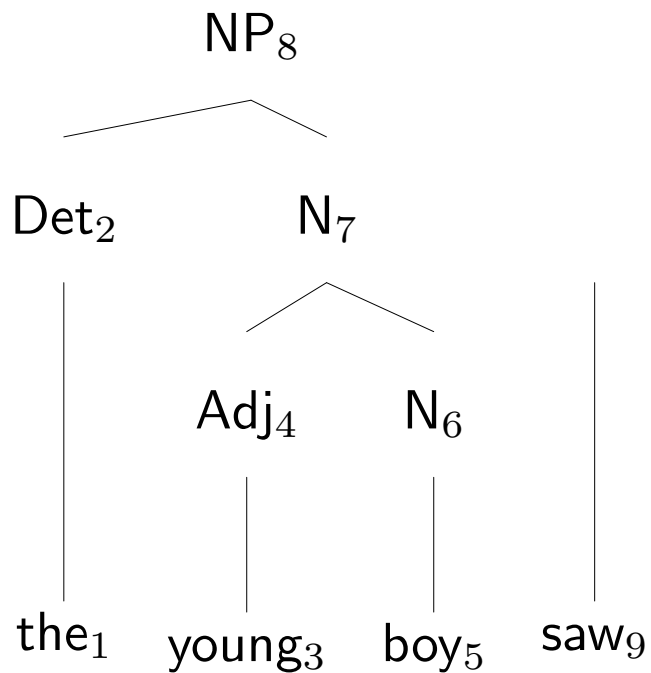
Bottom-up, left-right, depth-first tree traversal



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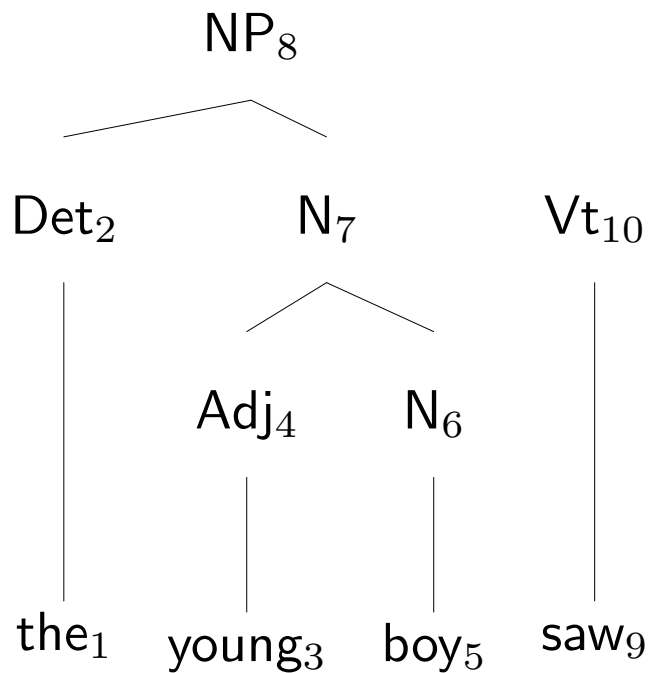
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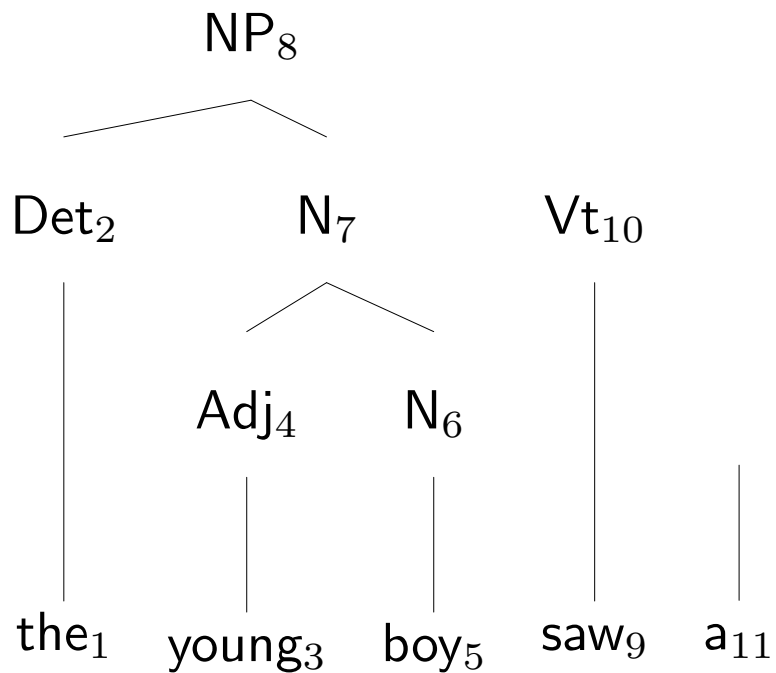
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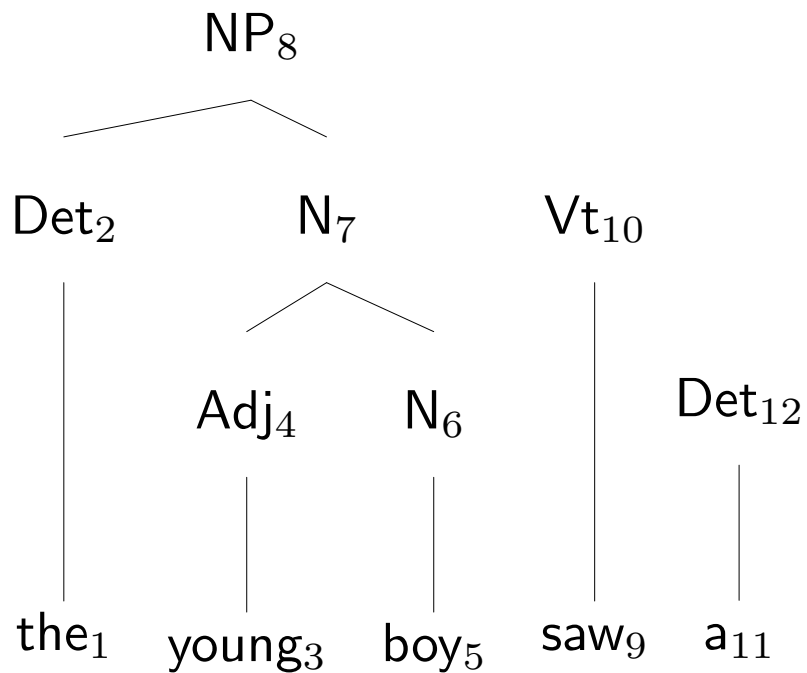
Bottom-up, left-right, depth-first tree traversal



S → NP VP
VP → Vt NP
NP → Det N
N → Adj N

Vt → saw
Det → the
Det → a
N → dragon
N → boy
Adj → young

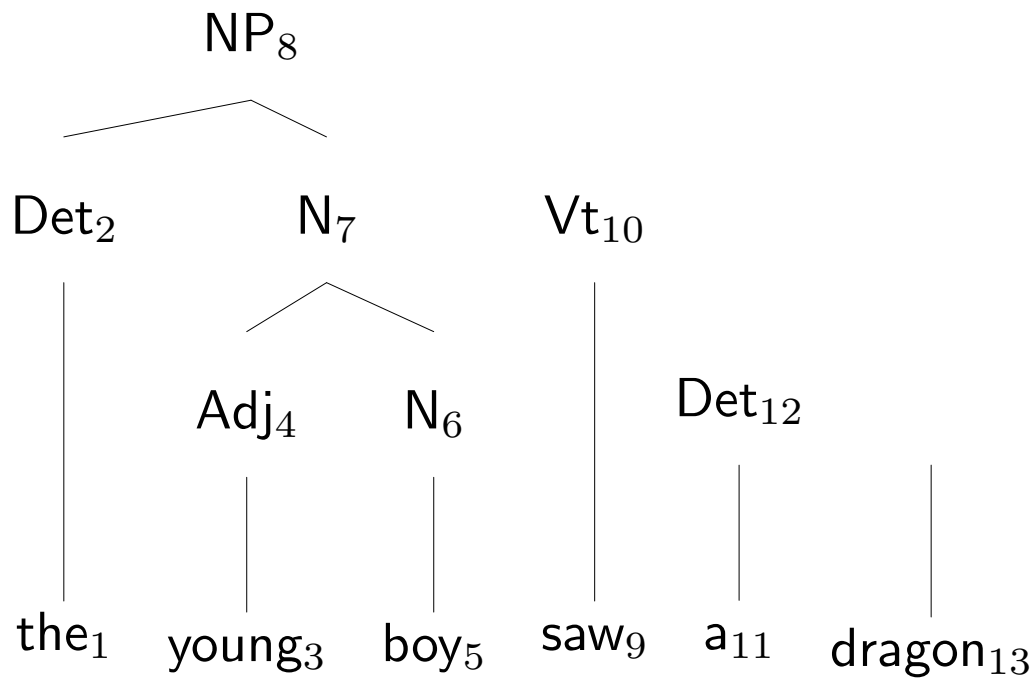
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 $N \rightarrow Adj N$

$Vt \rightarrow \text{saw}$
 $Det \rightarrow \text{the}$
 $Det \rightarrow \text{a}$
 $N \rightarrow \text{dragon}$
 $N \rightarrow \text{boy}$
 $Adj \rightarrow \text{young}$

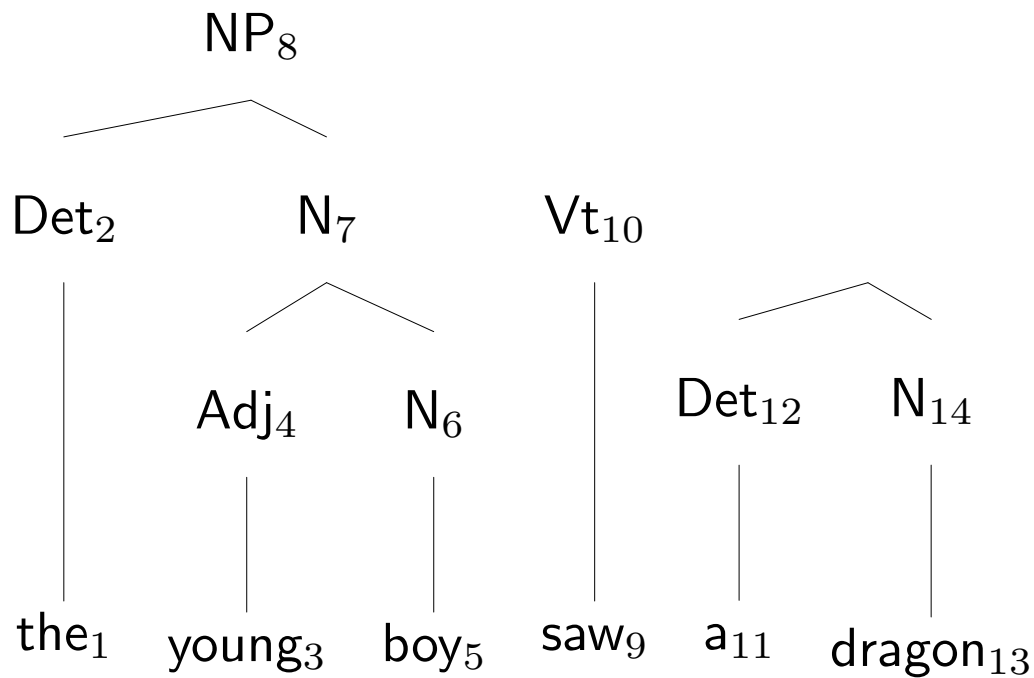
Bottom-up, left-right, depth-first tree traversal



$S \rightarrow NP VP$
 $VP \rightarrow Vt NP$
 $NP \rightarrow Det N$
 $N \rightarrow Adj N$

$Vt \rightarrow \text{saw}$
 $Det \rightarrow \text{the}$
 $Det \rightarrow \text{a}$
 $N \rightarrow \text{dragon}$
 $N \rightarrow \text{boy}$
 $Adj \rightarrow \text{young}$

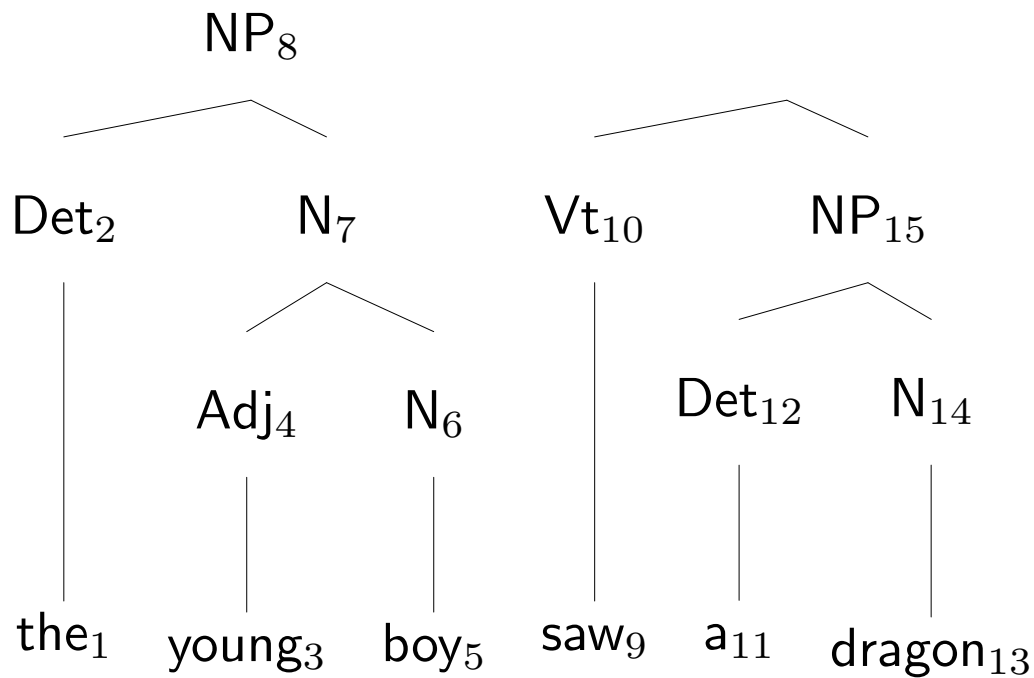
Bottom-up, left-right, depth-first tree traversal



$S \rightarrow NP VP$
 $VP \rightarrow Vt NP$
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$Vt \rightarrow \text{saw}$
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 $N \rightarrow \text{dragon}$
 $N \rightarrow \text{boy}$
 $Adj \rightarrow \text{young}$

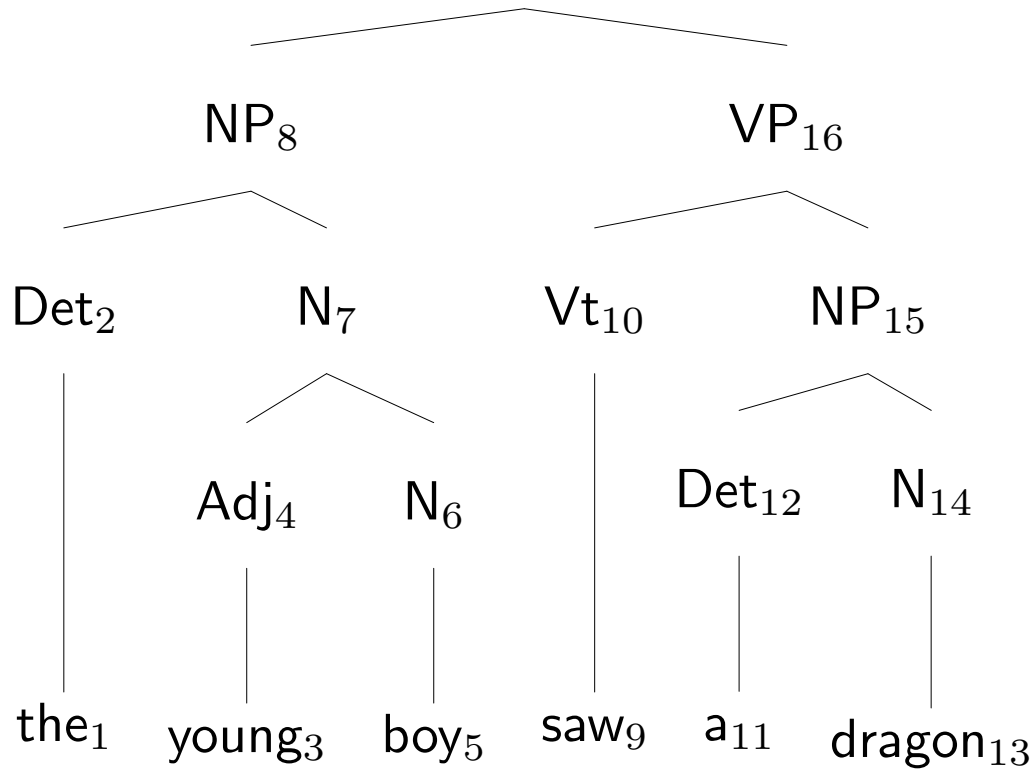
Bottom-up, left-right, depth-first tree traversal



$S \rightarrow NP VP$
 $VP \rightarrow Vt NP$
 $NP \rightarrow Det N$
 $N \rightarrow Adj N$

$Vt \rightarrow \text{saw}$
 $Det \rightarrow \text{the}$
 $Det \rightarrow \text{a}$
 $N \rightarrow \text{dragon}$
 $N \rightarrow \text{boy}$
 $Adj \rightarrow \text{young}$

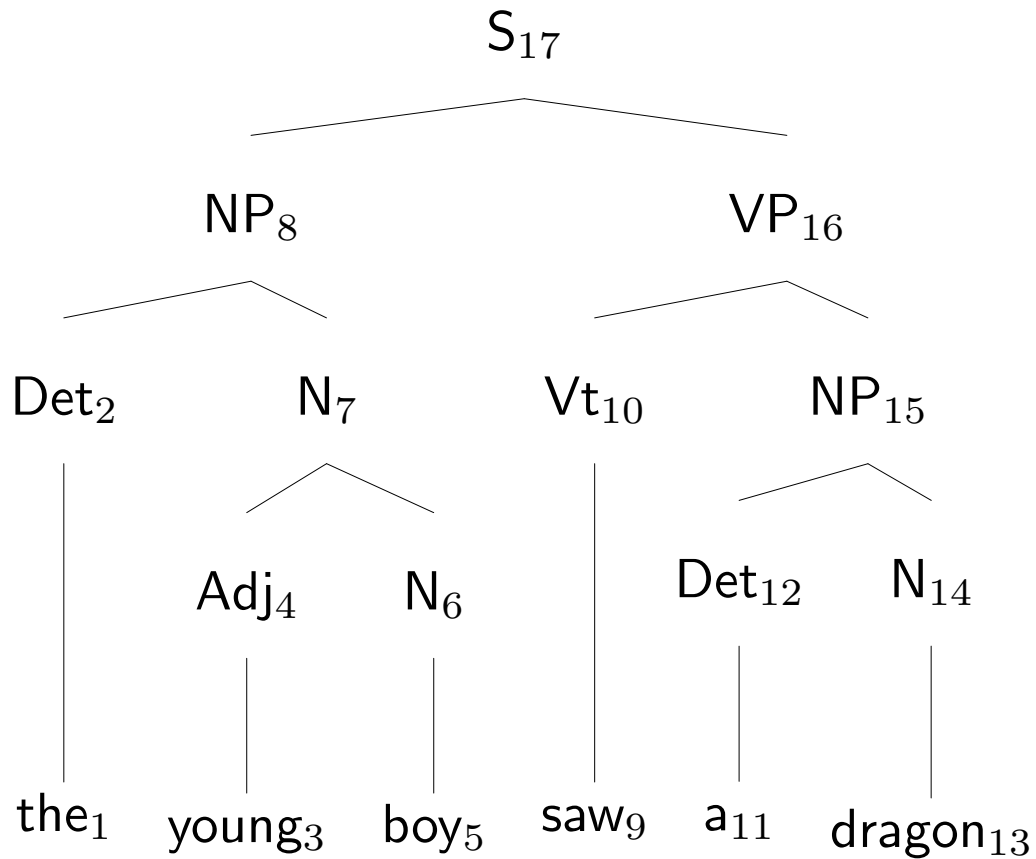
Bottom-up, left-right, depth-first tree traversal



$S \rightarrow NP VP$
 $VP \rightarrow Vt NP$
 $NP \rightarrow Det N$
 $N \rightarrow Adj N$

$Vt \rightarrow \text{saw}$
 $Det \rightarrow \text{the}$
 $Det \rightarrow \text{a}$
 $N \rightarrow \text{dragon}$
 $N \rightarrow \text{boy}$
 $Adj \rightarrow \text{young}$

Bottom-up, left-right, depth-first tree traversal



$S \rightarrow NP VP$
 $VP \rightarrow Vt NP$
 $NP \rightarrow Det N$
 $N \rightarrow Adj N$

$Vt \rightarrow \text{saw}$
 $Det \rightarrow \text{the}$
 $Det \rightarrow \text{a}$
 $N \rightarrow \text{dragon}$
 $N \rightarrow \text{boy}$
 $Adj \rightarrow \text{young}$

A trace (parser/simple/grammar.pl, parser/simple/sr_parser_trace.pl)

```
| ?- sr_parse([the,young,boy,saw,the,dragon]).  
START: <[],[the,young,boy,saw,the,dragon]>  
  Reduce []? no  
  Shift "the"  
<[the],[young,boy,saw,the,dragon]>  
  Reduce [the] => det  
<[det],[young,boy,saw,the,dragon]>  
  Reduce [det]? no  
  Reduce []? no  
  Shift "young"  
<[det,young],[boy,saw,the,dragon]>  
  Reduce [det,young]? no  
  Reduce [young] => adj
```

```
<[det, adj] , [boy, saw, the, dragon] >  
  Reduce [det, adj]? no  
  Reduce [adj]? no  
  Reduce []? no  
  Shift "boy"  
<[det, adj, boy] , [saw, the, dragon] >  
  Reduce [det, adj, boy]? no  
  Reduce [adj, boy]? no  
  Reduce [boy] => n  
<[det, adj, n] , [saw, the, dragon] >  
  Reduce [det, adj, n]? no  
  Reduce [adj, n] => n  
<[det, n] , [saw, the, dragon] >  
  Reduce [det, n] => np  
<[np] , [saw, the, dragon] >  
  Reduce [np]? no  
  Reduce []? no  
  Shift "saw"
```

```
<[np, saw] , [the, dragon]>
  Reduce [np, saw]? no
  Reduce [saw] => vt
<[np, vt] , [the, dragon]>
  Reduce [np, vt]? no
  Reduce [vt]? no
  Reduce []? no
  Shift "the"
<[np, vt, the] , [dragon]>
  Reduce [np, vt, the]? no
  Reduce [vt, the]? no
  Reduce [the] => det
<[np, vt, det] , [dragon]>
  Reduce [np, vt, det]? no
  Reduce [vt, det]? no
  Reduce [det]? no
  Reduce []? no
  Shift "dragon"
```

```
<[np, vt, det, dragon] , [] >
  Reduce [np, vt, det, dragon]? no
  Reduce [vt, det, dragon]? no
  Reduce [det, dragon]? no
  Reduce [dragon] => n
<[np, vt, det, n] , [] >
  Reduce [np, vt, det, n]? no
  Reduce [vt, det, n]? no
  Reduce [det, n] => np
<[np, vt, np] , [] >
  Reduce [np, vt, np]? no
  Reduce [vt, np] => vp
<[np, vp] , [] >
  Reduce [np, vp] => s
<[s] , [] >
SUCCESS!
```

A shift-reduce parser for grammars in CNF using difference lists to encode the string (parser/simple/cnf_sr.pl)

```
:- op(1100,xfx,'--->').
```

```
recognise(String) :- recognise([],String) % Start
```

```
recognise([s],[]). % Success
```

```
recognise([Y,X|Rest],S) :- % Reduce  
    (LHS ---> [X,Y]),  
    recognise([LHS|Rest],S).
```

```
recognise(Stack,[Word|S]) :- % Shift  
    Cat ---> [Word],  
    recognise([Cat|Stack],S).
```

A trace (parser/simple/grammar.pl, parser/simple/cnf_sr_trace.pl)

```
| ?- recognise([the,young,boy,saw,the,dragon]).  
START: <[],[the,young,boy,saw,the,dragon]>  
      Shift "the" as "det"  
<[det],[young,boy,saw,the,dragon]>  
      Shift "young" as "adj"  
<[adj,det],[boy,saw,the,dragon]>  
      Reduce [det,adj]? no  
      Shift "boy" as "n"  
<[n,adj,det],[saw,the,dragon]>  
      Reduce [adj,n] => n  
<[n,det],[saw,the,dragon]>  
      Reduce [det,n] => np  
<[np],[saw,the,dragon]>  
      Shift "saw" as "vt"
```



```
<[vt,np] , [the,dragon]>
  Reduce [np,vt]? no
  Shift "the" as "det"
<[det,vt,np] , [dragon]>
  Reduce [vt,det]? no
  Shift "dragon" as "n"
<[n,det,vt,np] , []>
  Reduce [det,n] => np
<[np,vt,np] , []>
  Reduce [vt,np] => vp
<[vp,np] , []>
  Reduce [np,vp] => s
<[s] , []>
SUCCESS!
```