

Implementing finite state machines and learning Prolog along the way

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OSU, LING 684.01

Overview

- A first introduction to Prolog
- Encoding finite state machines in Prolog
- Recognition and generation with finite state machines in Prolog
- Completing the FSM recognition and generation algorithms to use
 - ϵ transitions
 - abbreviations
- Encoding finite state transducers in Prolog

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The Prolog programming language (1)

PROgrammation LOGique was invented by Alain Colmerauer and colleagues at Marseille and Edinburgh in the early 70s. A Prolog program is written in a subset of first order predicate logic. There are

- **constants** naming entities
 - *syntax*: starting with lower-case letter (or number or single quoted)
 - *examples*: `twelve`, `a`, `q_1`, `14`, `'John'`
- **variables** over entities
 - *syntax*: starting with upper-case letter (or an underscore)
 - *examples*: `A`, `This`, `_twelve`, `_`
- **predicate symbols** naming relations among entities
 - *syntax*: predicate name starting with a lower-case letter with parentheses around comma-separated arguments
 - *examples*: `father(tom,mary)`, `age(X,15)`

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The Prolog programming language (2)

A Prolog program consists of a set of *Horn* clauses:

- **unit clauses** or **facts**
 - *syntax*: predicate followed by a dot
 - *example*: `father(tom,mary).`
- **non-unit clauses** or **rules**
 - *syntax*: `rel0 :- rel1, ..., reln.`
 - *example*: `grandfather(Old,Young) :-`
`father(Old,Middle),`
`father(Middle,Young).`

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The Prolog programming language (3)

- No global variables: Variables only have scope over a single clause.
- No explicit typing of variables or of the arguments of predicates.
- Negation by failure: For $\neg(P)$ Prolog attempts to prove P , and if this succeeds, it fails.

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A first Prolog program grandfather.pl

```
father(adam,ben).  
father(ben,claire).  
father(ben,chris).
```

```
grandfather(Old,Young) :-  
    father(Old,Middle),  
    father(Middle,Young).
```

Query:

```
?- grandfather(adam,X).  
X = claire ? ;  
X = chris ? ;  
no
```

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Recursive relations in Prolog Compound terms as data structures

To define recursive relations, one needs a richer data structure than the constants (atoms) introduced so far: *compound terms*.

A compound term comprises a functor and a sequence of one or more terms, the argument.¹ Compound terms are standardly written in prefix notation.²

Example:

- binary tree: `bin_tree(mother, l-dtr, r-dtr)`
- example: `bin_tree(s, np, bin_tree(vp,v,n))`

¹An atom can be thought of as a functor with arity 0.

²Infix and postfix operators can also be defined, but need to be declared.

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Recursive relations in Prolog Lists as special compound terms

- empty list: represented by the atom `[]`
 - non-empty list: compound term with `.` as binary functor
 - first argument: first element of list ("*head*")
 - second argument: rest of list ("*tail*")
- Example: `.(a, .(b, .(c, .(d, [])))`

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Abbreviating notations for lists

- bracket notation: `[element1 | restlist]`
Example: `[a | [b | [c | [d | []]]]]`
- element separator: `[element1 , element2]`
= `[element1 | [element2 | []]]`
Example: `[a, b, c, d]`

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An example for the four notations

```
[a,b,c,d] = .(a, .(b, .(c, .(d,[])))
= [a | [b | [c | [d | []]]]]
=
```

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Recursive relations in Prolog Example relations I: append

- Idea: a relation concatenating two lists
- Example: `?- append([a,b,c],[d,e],X) . => X=[a,b,c,d,e]`

```
append([],L,L).
append([H|T],L,[H|R]) :-
    append(T,L,R).
```

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Recursive relations in Prolog Example relations IIa: (naive) reverse

- Idea: reverse a list
- Example: `?- reverse([a,b,c],X) . => X=[c,b,a]`

```
naive_reverse([],[]).
naive_reverse([H|T],Result) :-
    naive_reverse(T,Aux),
    append(Aux,[H],Result).
```

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Recursive relations in Prolog Example relations IIb: reverse

```
reverse(A,B) :-
    reverse_aux(A,[],B).

reverse_aux([],L,L).
reverse_aux([H|T],L,Result) :-
    reverse_aux(T,[H|L],Result).
```

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Some practical matters

- To start Prolog on the Linguistics Department Unix machines:
 - SWI-Prolog: `p1`
 - SICStus: `prolog` or `M-x run-prolog` in XEmacs
- At the Prolog prompt (`?-`):
 - Exit Prolog: `halt.`
 - Consult a file in Prolog: `[filename].`³
- The manuals are accessible from the course web page.

³The `.pl` suffix is added automatically, but use single quotes if name starts with a capital letter or contains special characters such as `"` or `'`. For example `'MyGrammar'`, or `'~/file-1'`.

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Encoding finite state automata in Prolog What needs to be represented?

A finite state automaton is a quintuple (Q, Σ, E, S, F) with

- Q a finite set of states
- Σ a finite set of symbols, the alphabet
- $S \subseteq Q$ the set of start states
- $F \subseteq Q$ the set of final states
- E a set of edges $Q \times (\Sigma \cup \{\epsilon\}) \times Q$

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Prolog representation of a finite state automaton

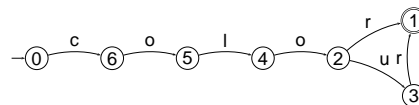
The FSA is represented by the following kind of Prolog facts:

- initial nodes: `initial(nodename).`
- final nodes: `final(nodename).`
- edges: `arc(from-node, label, to-node).`

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A simple example

FSTN representation of FSM:



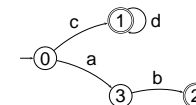
Prolog encoding of FSM:

```
initial(0).
final(1).
arc(0,c,6). arc(6,o,5). arc(5,l,4). arc(4,o,2).
arc(2,r,1). arc(2,u,3). arc(3,r,1).
```

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An example with two final states

FSTN representation of FSM:



Prolog encoding of FSM:

```
initial(0).
final(1). final(2).
arc(0,c,1). arc(1,d,1). arc(0,a,3). arc(3,b,2).
```

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Recognition with FSMs in Prolog fstm_traversal_basic.pl

```
test(Words) :-
    initial(Node),
    recognize(Node,Words).

recognize(Node,[]) :-
    final(Node).

recognize(FromNode,String) :-
    arc(FromNode,Label,ToNode),
    traverse(Label,String,NewString),
    recognize(ToNode,NewString).

traverse(First,[First|Rest],Rest).
```

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Generation with FSMs in Prolog

```
generate :-
    test(X),
    write(X),
    nl,
    fail.
```

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Encoding finite state transducers in Prolog What needs to be represented?

A finite state transducer is a 6-tuple $(Q, \Sigma_1, \Sigma_2, E, S, F)$ with

- Q a finite set of states
- Σ_1 a finite set of symbols, the input alphabet
- Σ_2 a finite set of symbols, the output alphabet
- $S \subseteq Q$ the set of start states
- $F \subseteq Q$ the set of final states
- E a set of edges $Q \times (\Sigma_1 \cup \{\epsilon\}) \times Q \times (\Sigma_2 \cup \{\epsilon\})$

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Prolog representation of a transducer

The only change compared to automata, is an additional argument in the representation of the arcs:

```
arc(from-node, label-in, to-node, label-out).
```

Example:

```
initial(1).
final(5).
arc(1,2,where,ou).
arc(2,3,is,est).
arc(3,4,the,la).
arc(4,5,exit,sortie).
arc(4,5,shop,boutique).
arc(4,5,toilet,toilette).
arc(3,6,the,le).
arc(6,5,policeman,gendarme).
```

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Processing with a finite state transducer

```
test(Input,Output) :-
    initial(Node),
    transduce(Node,Input,Output),
    write(Output),nl.

transduce(Node,[],[]) :-
    final(Node).

transduce(Node1,String1,String2) :-
    arc(Node1,Node2,Label1,Label2),
    traverse2(Label1,Label2,String1,NewString1,
              String2,NewString2),
    transduce(Node2,NewString1,NewString2).

traverse2(Word1,Word2,[Word1|RestString1],RestString1,
           [Word2|RestString2],RestString2).
```

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FSMs with ϵ transitions and abbreviations Defining Prolog representations

1. Decide on a symbol to use to mark ϵ transitions: '#'
2. Define abbreviations for labels:
macro(Label,Word).
3. Define a relation special/1 to recognize abbreviations and epsilon transitions:

```
special('#').
special(X) :-
    macro(X,_).
```

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FSMs with ϵ transitions and abbreviations Extending the recognition algorithm

```
test(Words) :-
    initial(Node),
    recognize(Node,Words).

recognize(Node,[]) :-
    final(Node).

recognize(FromNode,String) :-
    arc(FromNode,Label,ToNode),
    traverse(Label,String,NewString),
    recognize(ToNode,NewString).
```

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```
traverse(Label,[Label|RestString],RestString) :-
    \+ special(Label).
traverse(Abbrev,[Label|RestString],RestString) :-
    macro(Abbrev,Label).
traverse('#',String,String).

special('#').
special(X) :-
    macro(X,_).
```

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A tiny English fragment as an example (fsa/ex_simple_engl.pl)

```
initial(1).      arc(7,n,9).      macro(n,man).
final(9).        arc(8,adj,9).    macro(n,woman).
arc(1,np,3).     arc(8,mod,8).    macro(pv,is).
arc(1,det,2).   arc(9,cnj,4).    macro(pv,was).
arc(2,n,3).      arc(9,cnj,1).    macro(cnj,and).
arc(3,pv,4).     arc(3,pv,4).     macro(cnj,or).
arc(4,adv,5).   macro(np,kim).   macro(adj,happy).
arc(4,'#',5).   macro(np,sandy). macro(adj,stupid).
arc(5,det,6).   macro(np,lee).   macro(mod,very).
arc(5,det,7).   macro(det,a).    macro(adv,often).
arc(5,'#',8).   macro(det,the).  macro(adv,always).
arc(6,adj,7).   macro(det,her).  macro(adv,sometimes).
arc(6,mod,6).   macro(n,consumer).
```

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Reading assignment

- Pages 1–26 of Fernando Pereira and Stuart Shieber (1987): *Prolog and Natural-Language Analysis*. Stanford: CSLI.